



# LUSAS

*Engineering analysis and design software*



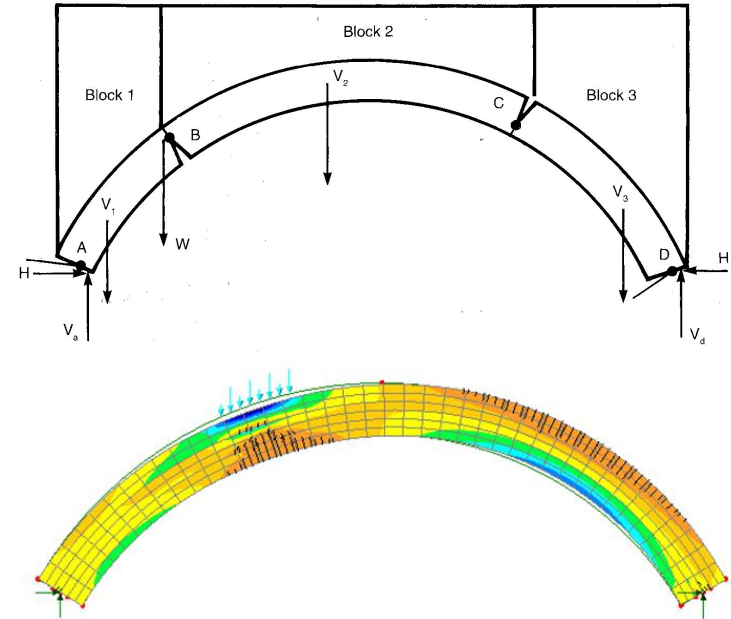
# Masonry arch modelling with LUSAS

Account Manager Name

Job Title, LUSAS

# Analysis of masonry arches

- [Introduction](#)
- Simple methods
  - [MEXE](#)
  - [Mechanism method](#)
- [FE analysis](#)
  - Cracking & crushing
  - Ring separation (delamination)
  - Soil/ structure interaction
- [Other masonry structures](#)



[End presentation](#)

# Introduction

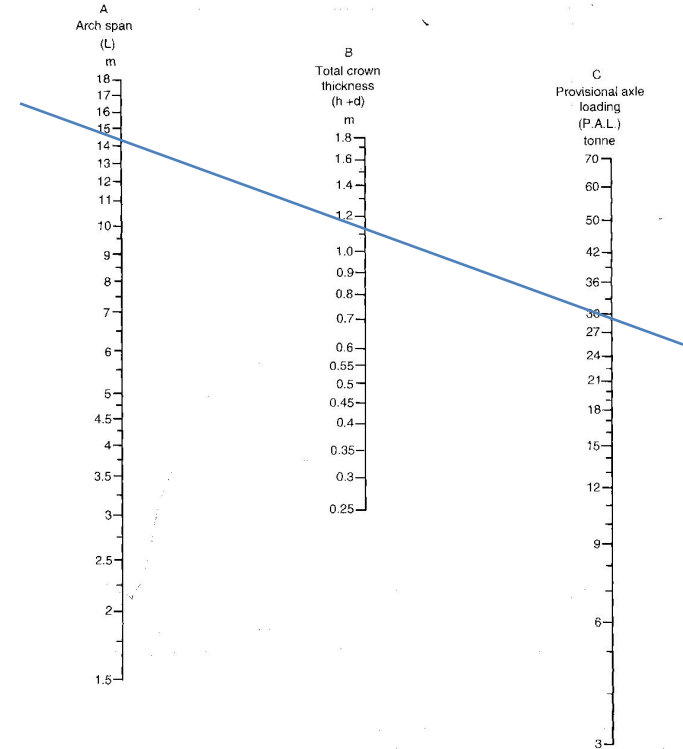
- Arch bridges - long history and very durable
- Still significant in the transport network
- Still being constructed
- China: 18 No. >100m span (since 1950)
- Analysis is potentially complicated
- Use LUSAS for simple or in-depth analysis



# MEXE (Empirical) (1/2)

Factors for

- Span to rise
- Profile
- Materials (barrel & fill)
- Joints (width, depth, mortar)
- Condition

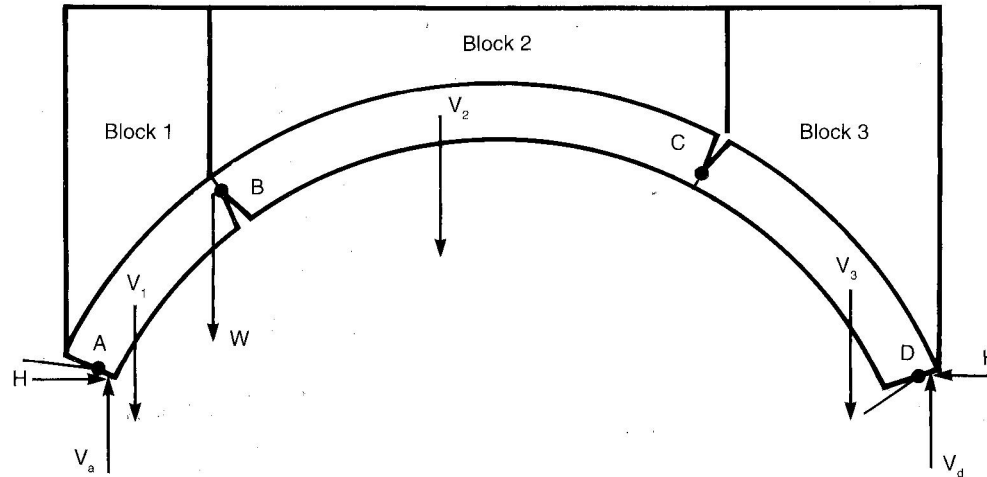


# MEXE (Empirical) (2/2)

- Based on gross assumptions & limited tests
- Limited accuracy for
  - Small spans
  - Large depth of fill
  - Mis-shapen arches or gothic arches etc
- No account of ring separation
  - No transverse effects or spandrel walls
- Not applicable to multiple spans or skews

# Mechanism methods (1/4)

- Hinges form at intrados or extrados
- 4 hinges form a mechanism



# Mechanism methods (2/4)

Pippard's assumptions:

- No tension
- Infinite compressive strength
- Infinite elastic modulus
- No sliding between blocks
- No structural contribution from the fill

Upper bound theory (“unsafe method”) – the lowest upper bound solution is sought



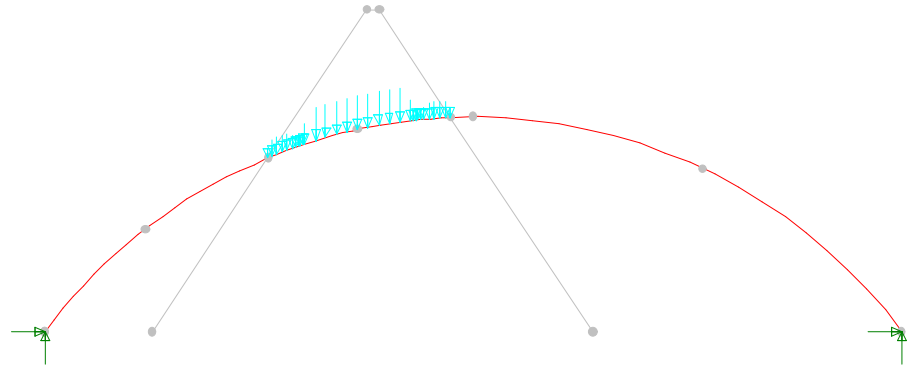
# Mechanism methods (3/4)

- Plastic “hinge” analysis could be carried out in LUSAS
- Modelling could be automated using VBScripting

**Arch Dimensions**

Arch Barrel Thickness	1.72
Fill Depth	5.3
Arch Rise at Center	4.10
Arch Rise at quarter points	3.95
Total Span	7.8

OK Cancel



# Mechanism method (4/4)

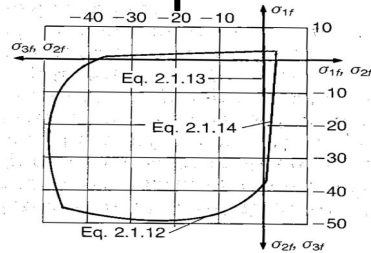
- LUSAS advantages:
  - No limit to shape of arch
  - Can carry out on 3D basis & skews
  - Can adjust support conditions
  - Can include backfill as load/ spring support
- The method does not address
  - ring separation
  - soil-structure interaction

# FE analysis

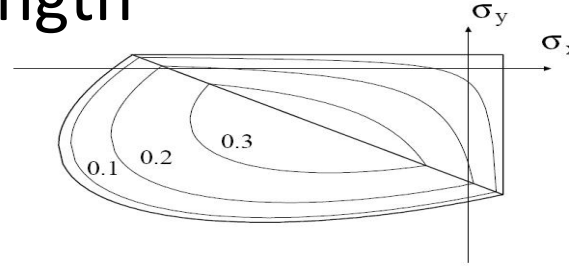
- Cracking & crushing in barrel
- Ring separation
- Soil/ structure interaction
- Geometric nonlinearity

# Concrete and masonry (1/3)

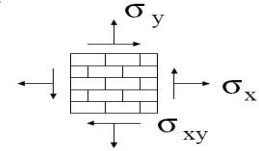
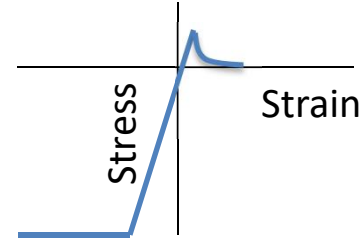
- Brittle fracture
- Low tensile strength, high compressive strength



CEB-FIP failure envelope for concrete

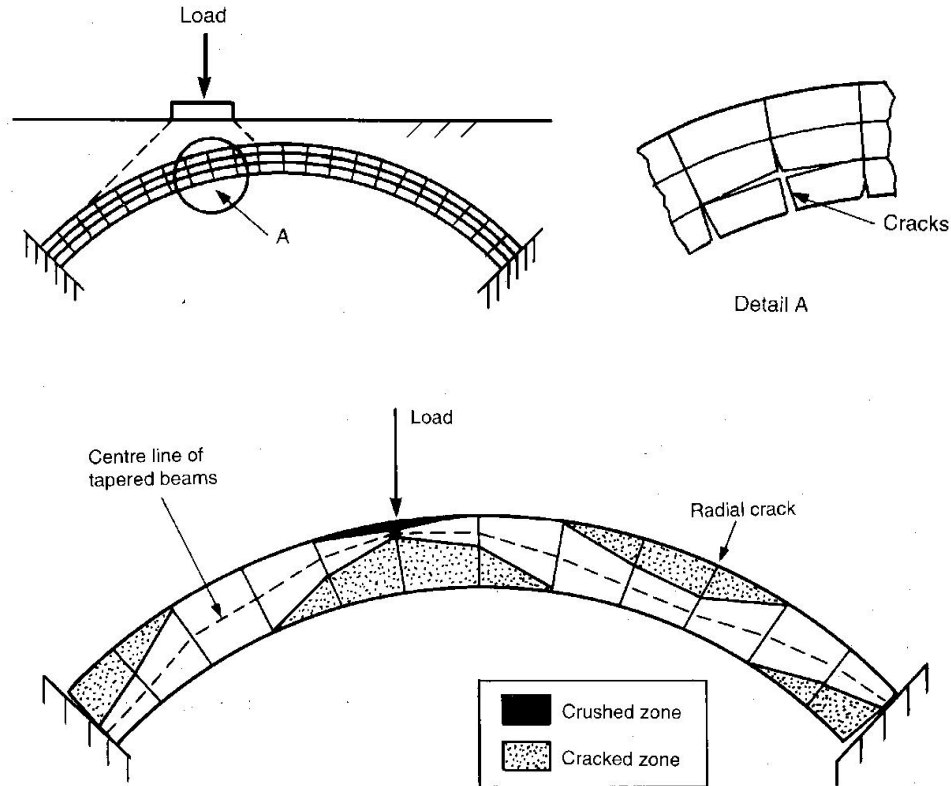


Rankine-Hill failure envelope for masonry



- Can use LUSAS advanced concrete material

# Cracking and crushing (2/3)



# Cracking and crushing (3/3)

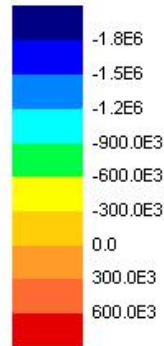
Loadcase: 2: Increment 2 Load Factor = 1.00000

Results file: Heyman by cracking.mys

Entity: Stress - Plane Strain

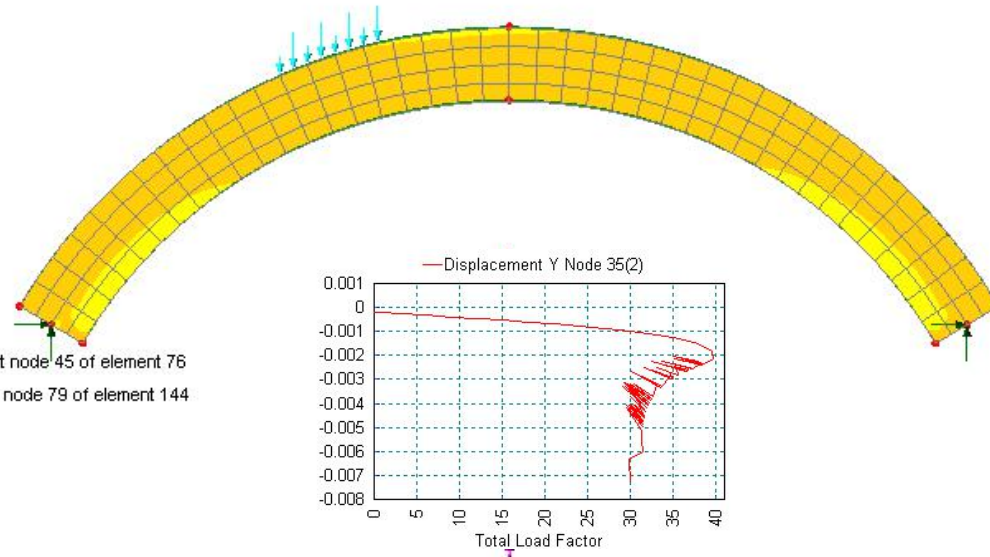
Transformation LocalRadial system

Component: St



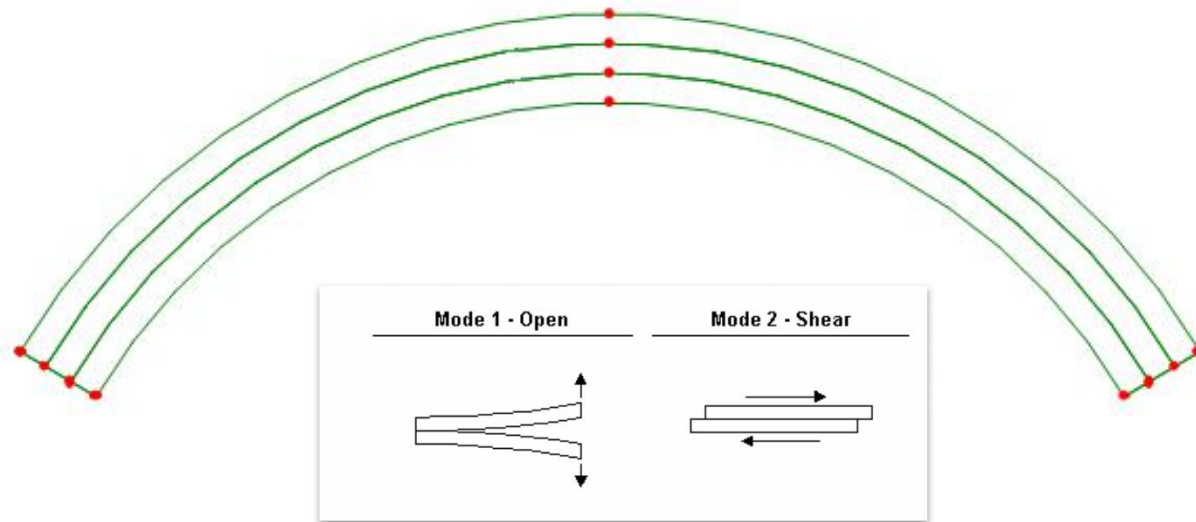
Maximum -4.20888E3 at node 45 of element 76

Minimum -429.794E3 at node 79 of element 144

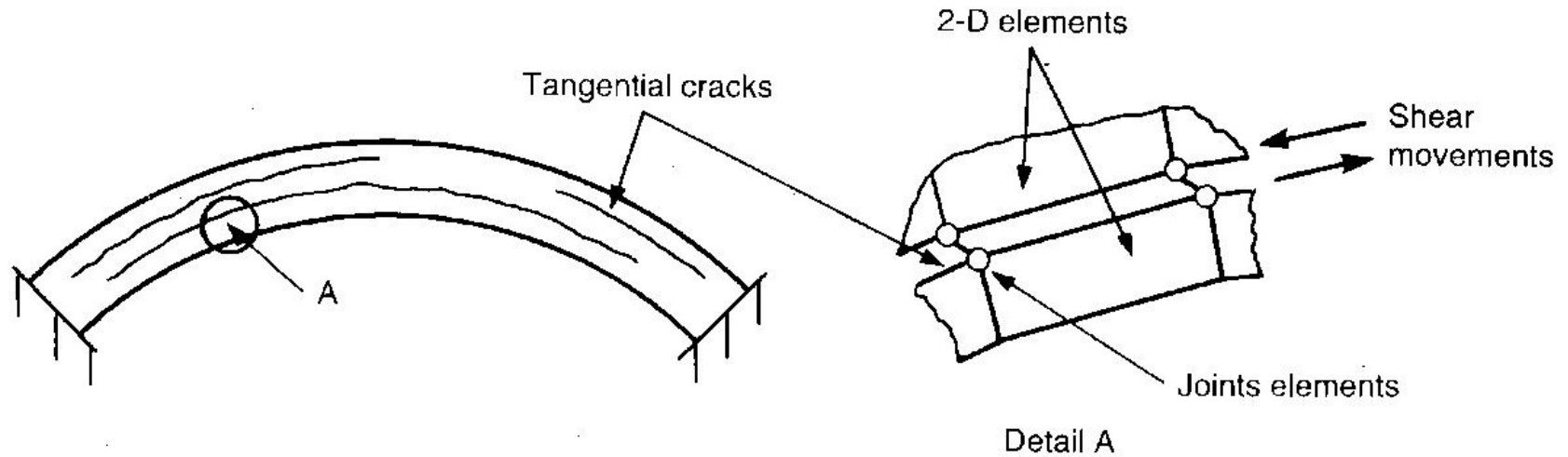


# Ring separation (1/5)

- Using cracking & crushing material
- Introduce interface elements. 2D or 3D



# Ring separation (2/5)





# Ring separation (3/5)

Loadcase: 2: Increment 2 Load Factor = 1.00000

Results file: Heyman Ring Separation with cracking.mys

Entity: Stress - Plane Strain

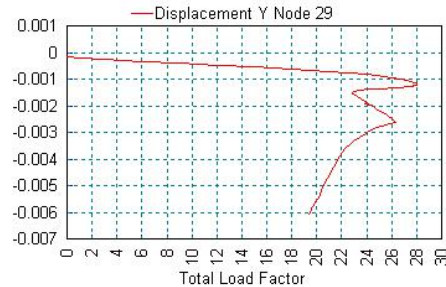
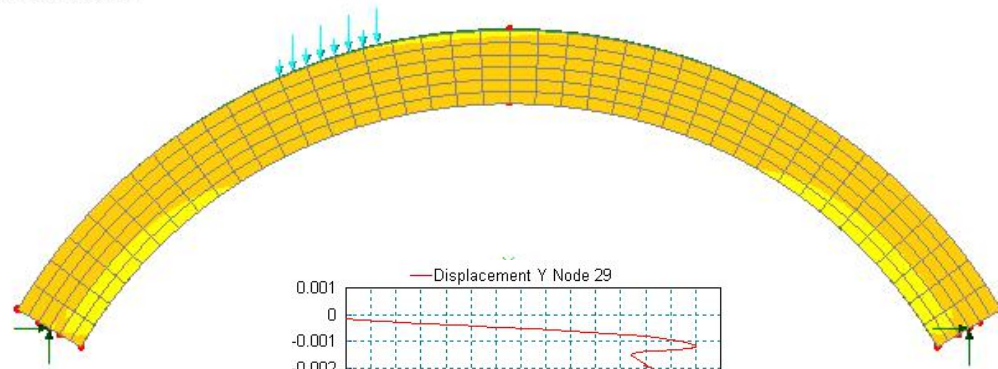
Transformation Local/Local Coordinates 1

Component: St



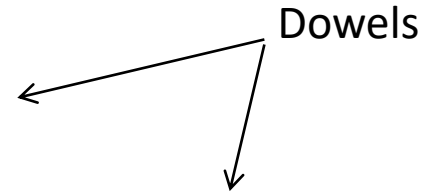
Maximum -3.68125E3 at node 39 of element 19

Minimum -430.782E3 at node 73 of element 36



# Ring separation/repairs (4/5)

- Can model defects and/ or repairs e.g. Dowels using joints or constraint equations



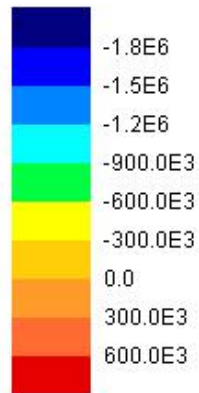
# Ring separation/repairs (5/5)

Loadcase: 2:Increment 2 Load Factor = 1.00000

Results file: Pinned arch with dowels constraint.mys

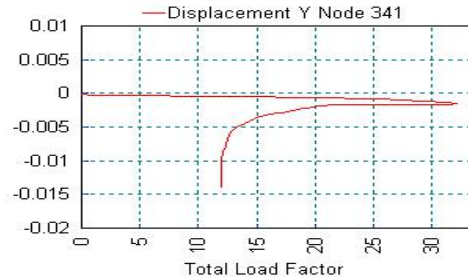
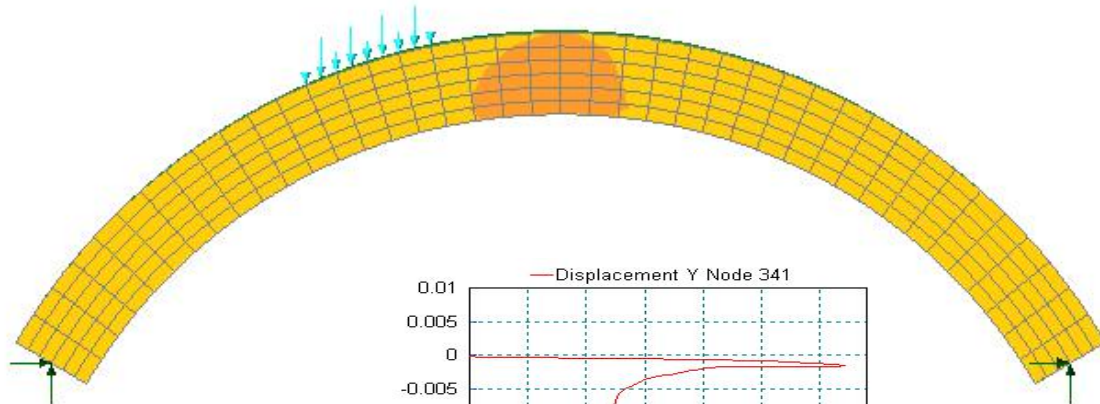
Entity: Stress - Plane Strain

Component: St



Maximum 17.1837E3 at node 944 of element 234

Minimum -253.06E3 at node 915 of element 226



# Defects and repairs

- Can model in 3D
- Good for skews

# Soil-structure interaction (1/2)

- Include backfill and surrounding structure
- Soil material models including Mohr-Coulomb

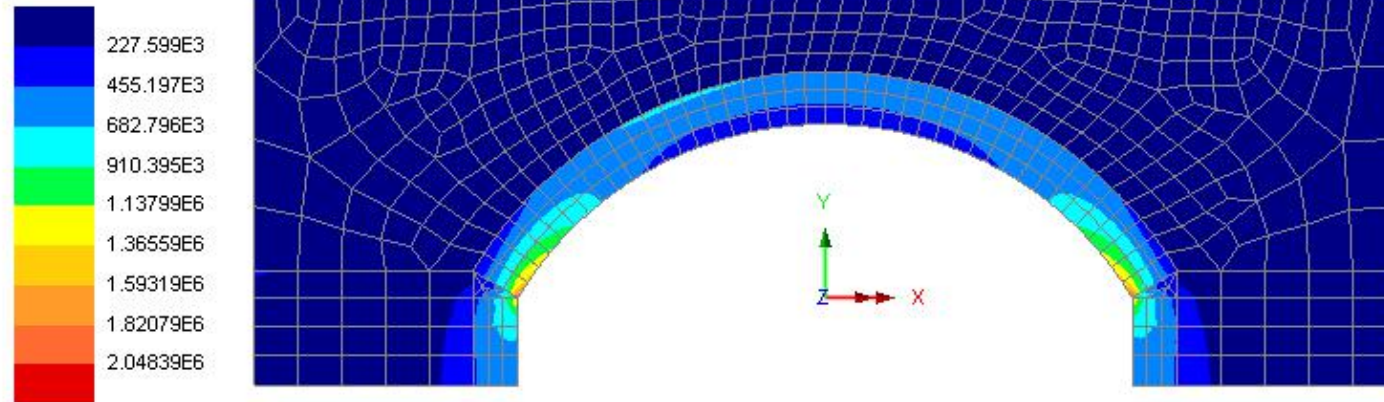
# Soil-structure interaction (2/2)

Loadcase: 2:Increment 2 Load Factor = 1.00000

Results file: Fill model with cracking.mys

Entity: Stress - Plane Strain

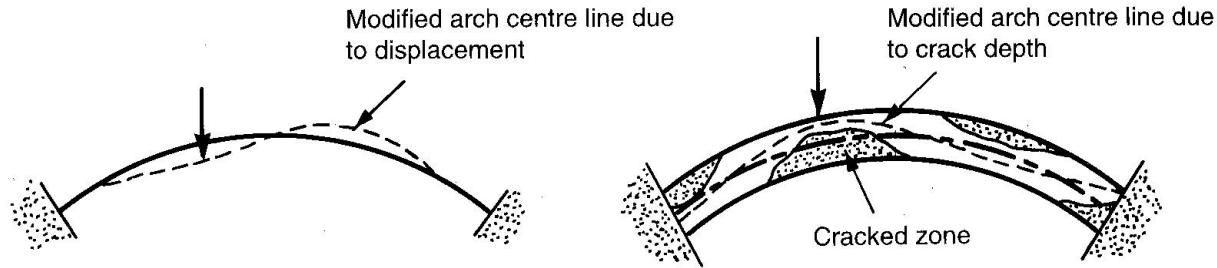
Component: SE



Maximum 2.04895E6 at node 1 of element 13

Minimum 557.705 at node 876 of element 233

# Geometric nonlinearity (1/1)



	2D (Plane strain)	3D continuum
Concrete model 94	Yes	Yes
Mohr Coulomb etc	Yes	Yes
Compatible Joints	Yes	Yes
Geometric NL	Yes	Yes

# Benefits of using LUSAS

- LUSAS analysis includes:
  - State of the art crushing/ cracking material
  - Ring separation using slidelines or joints
  - NL soil materials for fill
  - Soil/ structure interface
  - Geometric nonlinearity
  - Complete flexibility of geometry, materials, support conditions e.g. to include haunches/ spandrels etc.
  - Full 3D modelling (if required)
  - Ability to model defects and repairs



# Independent validation cases

## Finite-element analysis of masonry arch bridges

*K. H. Ng, BEng, C. A. Fairfield, BEng, PhD, MIHT, MInstNDT, and A. Sibbald, BSc, MSc, PhD, CEng, MICE, FInstNDT*

■ This paper describes a method of assessing the load-carrying capacity of masonry arch bridges using the general-purpose finite-element (FE) package LUSAS. Good agreement was found, in terms of collapse loads and load-deflection characteristics, between the FE analysis adopted here and the experimental data. Three bridges were assessed: Bridgemill (actual collapse load 361 kN/m, FE collapse load 362 kN/m), Strathmashie (actual collapse load 228 kN/m, FE collapse load 226 kN/m), and Barlae (actual collapse load 296 kN/m, FE collapse load 302 kN/m). These values were based on cases where the material properties were well documented, which will not always be the case for other less well-researched arches, and therefore a

parametric study involving the analysis of the arch bridge stock to allow increases in the maximum allowable gross vehicle weight (GVW) from 38 t to 40 t (certain bridges may have to be assessed for 44 t GVW) and in the maximum axle weight from 10 t to 11.5 t. Full-scale tests suggest that the MEXE method gives conservative results, with the consequence of heavy goods vehicles taking longer trips than would otherwise be required. This shifts traffic to bridges rated for the higher axle limits, thus speeding their deterioration. The actual safety factor on an arch bridge is very hard to find accurately by any of the current assessment methods; hence the current interest in arch analyses.

3. In this study a two-dimensional analysis was performed using LUSAS, a commercially available finite-element (FE) package.<sup>3</sup> Three full-scale bridge collapse tests were modelled

*Proc. Instn Civ. Engrs Structs & Bldgs, 1999, 134, May, 119–127*

*Paper 11789*

*Written discussion closes 27 August 1999*



*K. H. Ng, Postgraduate student, Department of Civil Engineering*

Proceedings of the Institution of Civil Engineers, Structures & Buildings Issue 134

# Other masonry structures (1/4)

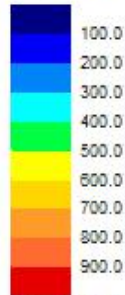
- Plate and shell models
- Orthotropic materials (linear and NL)
- Contact slidelines

# Other masonry structures (2/4)

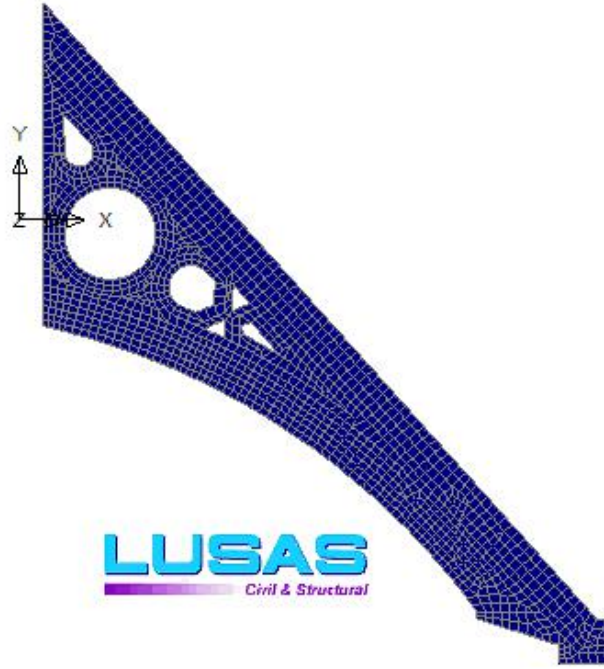


# Other masonry structures (3/4)

Loadcase: 2  
Title: Increment 2  
Results File: 0  
Entity: Stress  
Component: SE

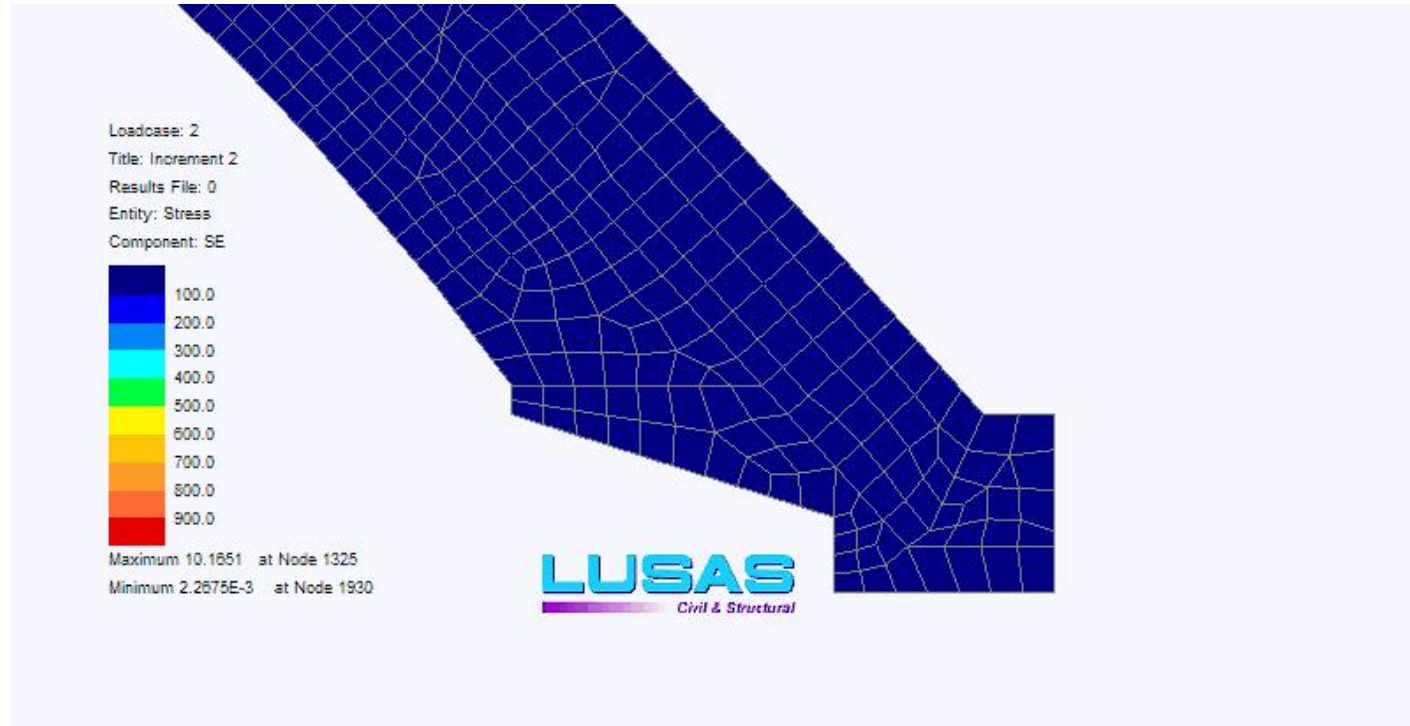


Maximum 10.1651 at Node 1325  
Minimum 2.2675E-3 at Node 1930



**LUSAS**  
Civil & Structural

# Other masonry structures (4/4)



# Why use LUSAS for Masonry structures?

- Flexible: simple or advanced approaches
- 2D or 3D, applicable to any shape
- State-of-the-art cracking and crushing
- Delamination interfaces and slidelines
- Soil-structure interaction
- Orthotropic materials

*Civil and Structural  
engineering*

*Bridge  
engineering*

*Composites  
engineering*

# LUSAS

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Applications*

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Research*

*General mechanical  
engineering*

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